

# S'entraîner 41 page 207

*Sésamath*

Maths 1S



- 1 Calculer  $\sin \frac{5\pi}{4}$ ,  $\sin \left(-\frac{\pi}{4}\right)$  et  $\sin \frac{5\pi}{6}$ .
- 2 On sait que  $\cos \left(\frac{2\pi}{5}\right) = \frac{\sqrt{5} - 1}{4}$ .  
En déduire  $\sin \left(\frac{\pi}{10}\right)$ .

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